

Cambridge International AS & A Level

---

<https://babacambridgesolutions.com>

Mathematics

9709/32

Paper 3 Pure Mathematics 3

May/June 2023

Question No (2)

- 2 Solve the equation  $\ln(2x^2 - 3) = 2 \ln x - \ln 2$ , giving your answer in an exact form.

**Solution:**

$$\ln(2x^2 - 3) = 2 \ln x - \ln 2$$

Formula for  $\ln$

$$\textcircled{1} \ln(xy) = \ln x + \ln y$$

$$\textcircled{2} \ln x^n = n \ln x$$

$$\ln(2x^2 - 3) = \ln x^2 - \ln 2$$

$$\ln(2x^2 - 3) = \ln\left(\frac{x^2}{2}\right)$$

$$\Rightarrow 2x^2 - 3 = \frac{x^2}{2}$$

$$2(2x^2 - 3) = x^2$$

$$4x^2 - 6 = x^2$$

$$4x^2 - x^2 = 6$$

$$3x^2 = 6$$

$$x^2 = 2$$

$$x = \sqrt{2}$$

Removing  $\ln$

$$\because e^{\ln} = 1$$

$-\sqrt{2}$  is  
undefined  
in  $\ln$ .

