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Mathematics

9709/32

Paper 3 Pure Mathematics 3

May/June 2023

Question No (1)

1 Solve the inequality $|5x - 3| < 2|3x - 7|$.

Solution:

$$|5x - 3| < 2|3x - 7|$$

$$\Rightarrow (5x - 3)^2 < 2^2 (3x - 7)^2 \quad \text{Squaring}$$

$$25x^2 - 30x + 9 < 4(9x^2 - 42x + 49)$$

$$25x^2 - 30x + 9 - 36x^2 + 168x - 196 < 0$$

$$-11x^2 + 138x - 187 < 0$$

$$11x^2 - 138x + 187 > 0 \quad \because \text{if } -a < 0$$

Solving by 3 term quadratic and factorization $-x - a > -x + a$
 $a > 0$

$$\left(x - \frac{17}{11}\right)(x - 11) > 0$$

but above inequality satisfy only for

$$\left(x - \frac{17}{11}\right) < 0 \quad , \quad (x - 11) > 0$$

$$x < \frac{17}{11} \quad , \quad x > 11$$

So the answer is $x < \frac{17}{11}$, $x > 11$

