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Mathematics

9709/52

Paper 5 Probability & Statistics 1

October/November 2025

Question No (1)

- 1** A coin is biased so that the probability of obtaining a head when it is thrown is 0.4. The coin is thrown repeatedly until the first head is obtained.
- (a) Find the probability that the first head is obtained on the 5th throw.
- (b) Find the probability that the first head is obtained after the 6th throw.

Solution:

(a)

It's about the geometric distribution

By given conditions

$$P(H) = 0.4$$

$$P(T) = 1 - 0.4 = 0.6 \quad \checkmark \text{ 1 is total probability}$$

(First head occurs on the 5th throw means first 4 throws must be tail and 5th throw must be head)

$$\begin{aligned} P(\text{first head on 5th}) &= q^4 p \\ &= (0.6)^4 \cdot 0.4 \\ &= 0.05184 \end{aligned}$$

(b)

$$P(H) = 0.4$$

$$P(T) = 1 - 0.4$$

$$P(T) = 0.6$$

$$P(\text{first head after 6th throw}) = 1 - (P + Pq + Pq^2 + Pq^3 + Pq^4 + Pq^5)$$

$$= 1 - (0.4 + (0.4)(0.6) + (0.4)(0.6)^2 + (0.4)(0.6)^3 + (0.4)(0.6)^4 + (0.4)(0.6)^5)$$
$$= 0.0467$$